

## INTRODUCTION

### What are binary star systems?

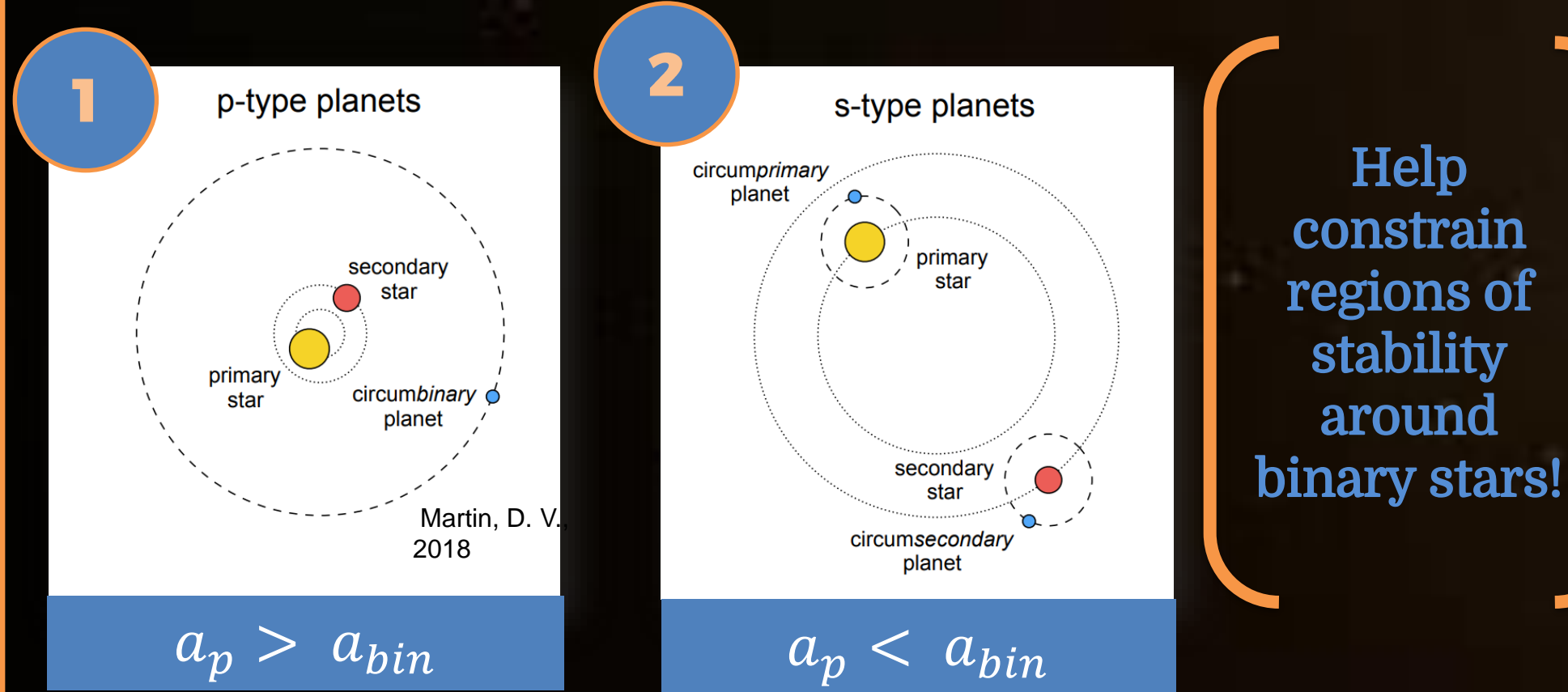
A Binary Star System is a system consisting of 2 stars orbiting a common center of mass

### Why are they important?

- Most observable stars are in binaries<sup>1</sup>
- Serve as one of the best methods to determine mass of distant stars<sup>2</sup>
- Provide important clues about the conditions under which stars are formed<sup>2</sup>

### Two main planetary orbital configurations:

- 1) Circumbinary planets ( p-type orbitals )
- 2) Circumstellar planets ( s-type orbitals )



## OBJECTIVE

Conduct survival analysis to obtain a more reliable stability criterion for circumbinary planets/test particles in N-body simulations

## METHODOLOGY

### ❖ How did we study these systems?

- Run N-body simulations REBOUND software package
- Observe long term stability of test particles under different orbital constraints (time of particle ejection)

#### Orbital elements:

- Binary eccentricity ( $e_b$ ): 0.0-0.7
- Test particle semi major axis ( $a_p$ ): 1.0-5.0
- Binary reduced mass ( $\mu$ ): 0.05 - 0.5
- # of test particles/simulation ( $N_p$ ): 10-30

- Compare to results from previous studies: Critical Semimajor Axis ( $a_{crit}$ )<sup>3</sup>

$$\frac{a_{crit}}{a_{bin}} = 1.60 + 5.10e_{bin} - 2.22e_{bin}^2 + 4.12\mu_{bin} - 4.27e_{bin}\mu_{bin} - 5.09\mu_{bin}^2 + 4.61e_{bin}^2\mu_{bin}^2$$

Holman & Wiegert (1999) (1)

### ❖ How do we constrain particle survival times?

- Survival Analysis (SA) : deals with estimation of right-censored data LIFELINES software package

- Two (2) main functions:

1. Survival Function (SF):

$$S(t) = Pr(T > t)$$

2. Hazard Function (HF):

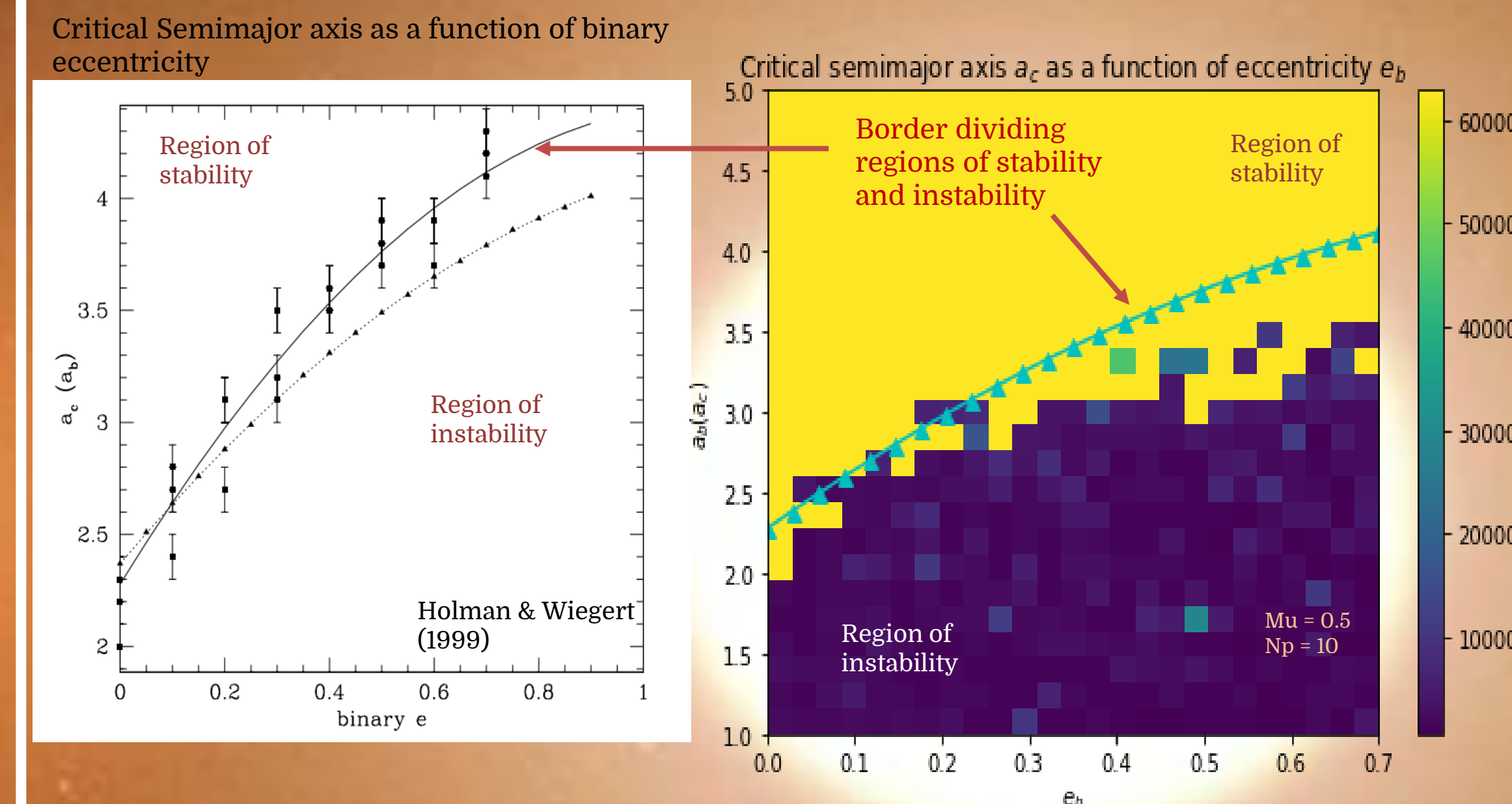
$$h(t) = \lim_{\delta t \rightarrow 0} \frac{Pr(t \leq T \leq t + \delta t | T > t)}{\delta t}$$

Probability of surviving past time  $t$

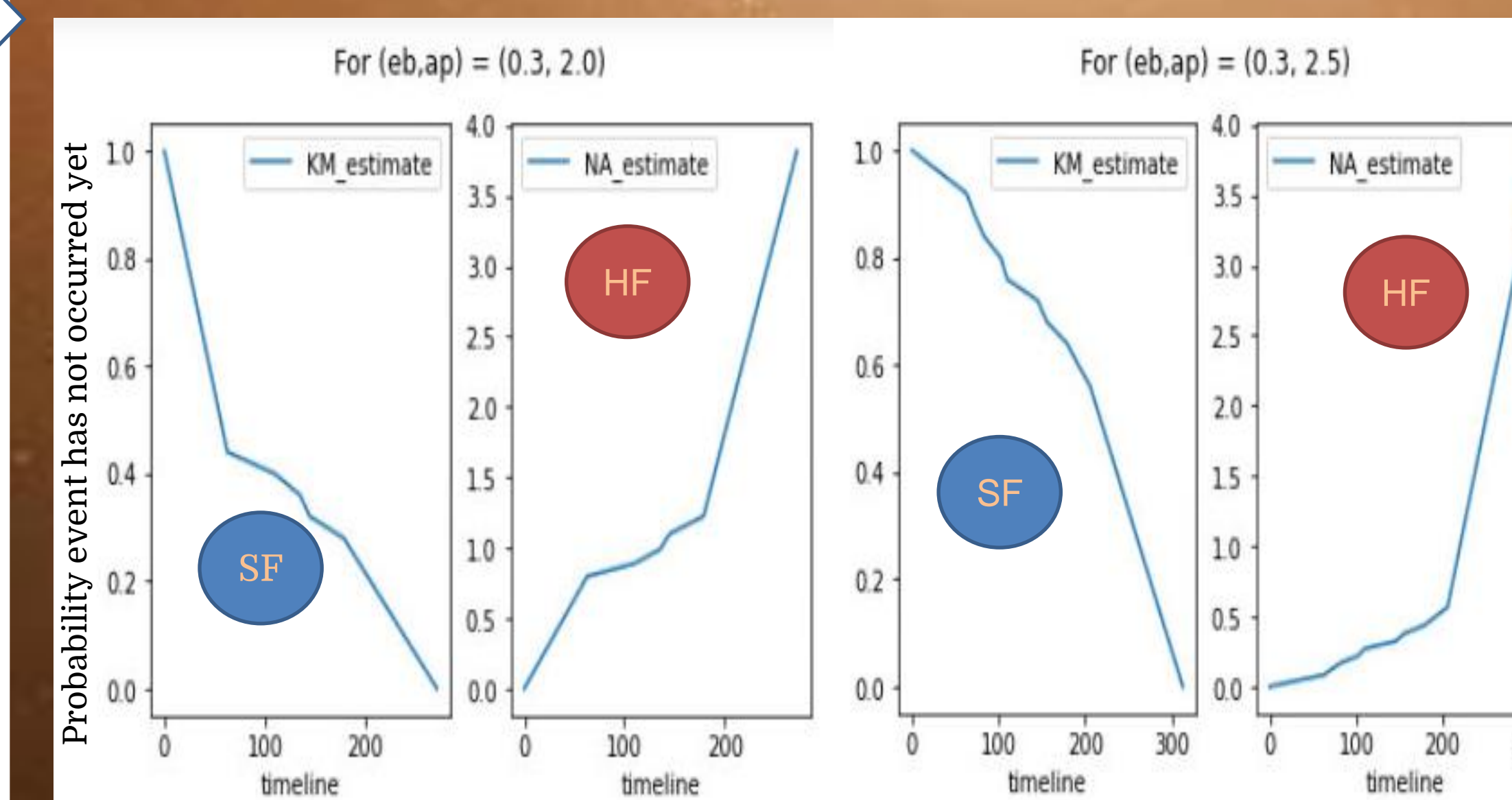
Probability of ejection at time  $t$ , given the ejection has not occurred yet

## FINDINGS THUS FAR...

- Trend line of orbital stability agrees with previous studies (Holman & Wiegert 1999)



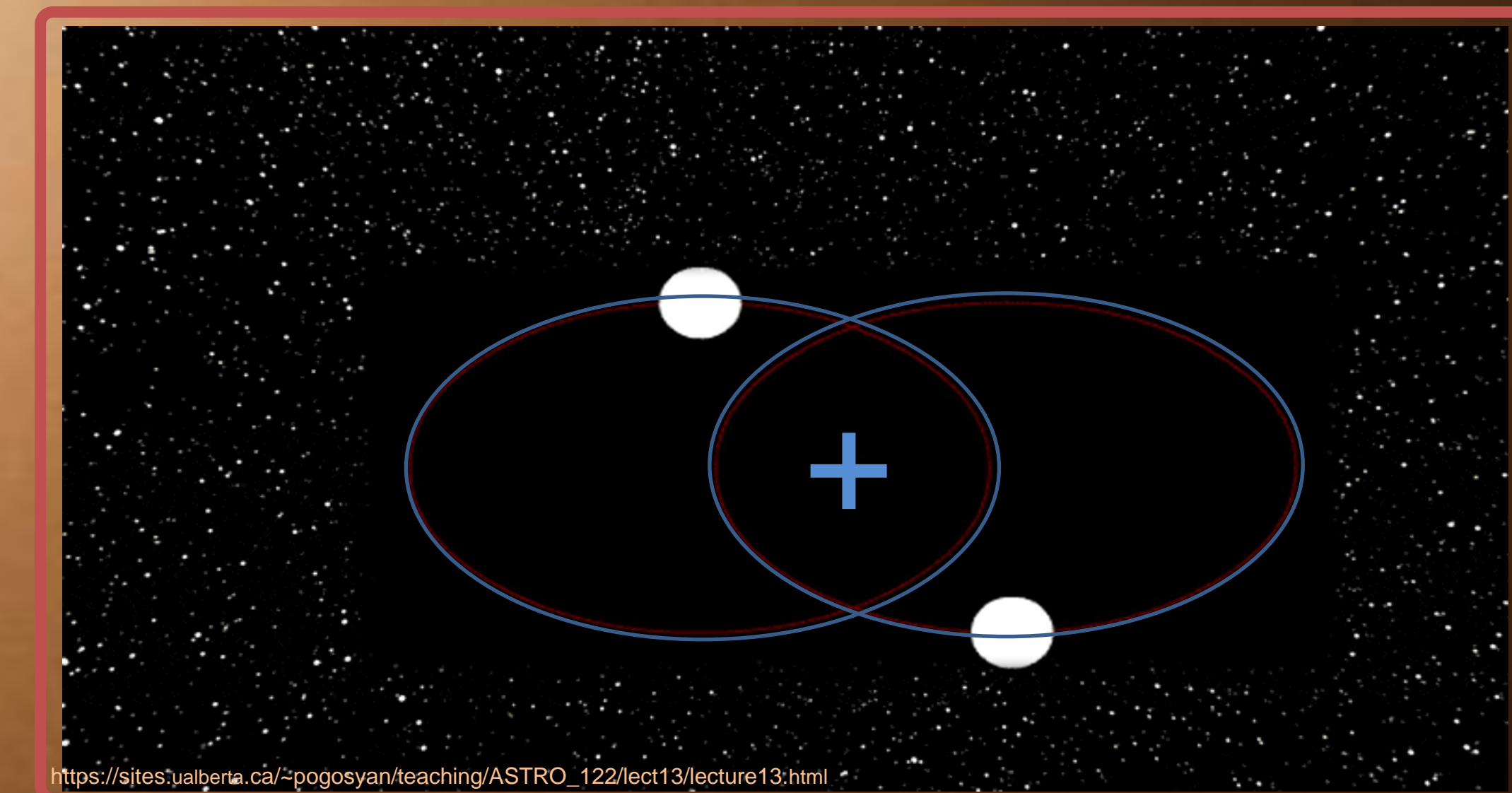
- Survival & Hazard functions for specific orbital elements (provide a better estimate of test particle survival times)



## NEXT STEPS

In the future we aim to:

- 1) Apply survival and hazard functions to all data sets obtained
- 2) Incorporate Survival Regression in our statistical analysis of survival times
- 3) Conduct simulations for a larger range of binary mass ratios
- 4) Study the effects of Tidal dissipation on binary stability (See Kanah Smith's poster!)



## REFERENCES

- 1) Martin, D. V. (2018). *Populations of Planets in Multiple Star Systems* (pp. 2035-2060), Springer International Publishing. [http://dx.doi.org/10.1007/978-3-319-55333-7\\_153](http://dx.doi.org/10.1007/978-3-319-55333-7_153)
- 2) Milone, E. F., Leahy, D. A., & Hobill, D. W. (2008). *Short-Period Binary Stars: Observations, Analyses, and Results* (1st ed. 2008.). Springer Netherlands. <https://doi.org/10.1007/978-1-4020-6544-6>
- 3) Holman & Wiegert (1999)